Numerical investigation of dynamic embedment of offshore pipelines

Étude numérique de l'ancrage dynamique de conduites enterrées maritimes

Dutta S., Hawlader B.
Memorial University, St. John's, Canada.

Phillips R.
C-CORE, St. John's, Canada.

ABSTRACT: Pipelines are one of the key components of offshore oil and gas development programs. Deep water pipelines are often laid on the seabed and penetrate into soil a fraction of their diameter. High operating temperature and pressure generate axial stress that could buckle the pipeline laterally. The embedment and formation of soil berm have a significant effect on lateral resistance. The embedment of a pipeline depends on stress concentration at the touchdown point (TDP) and dynamic laying effects. In this study, large deformation finite element modelling of dynamic penetration of offshore pipeline is presented. The Coupled Eulerian Lagrangian (CEL) technique is used to develop finite element model. The pipe is first penetrated into the seabed followed by a small amplitude cyclic lateral motion. Results from the finite element models are compared with centrifuge test results. High plastic shear strain is obtained around the pipeline during cyclic loading which causes significant pipe embedment. The shape of soil berm is different from that of monotonic pipe penetration.

RÉSUMÉ : Les conduites enterrées sont un des éléments clés des programmes de développement de pétrole et de gaz. Des conduites enterrées en eau profonde sont souvent mises sur le plancher océanique et pénètrent dans le sol sur une fraction de leur diamètre. La température et la pression de fonctionnement élevées génèrent une contrainte axiale qui peuvent déformer la conduite latéralement. L'ancrage et le sol encaissant ont un effet significatif sur la résistance latérale. L'enfouissement d'une conduite dépend des concentrations de contraintes et des effets dynamiques de la pose. Dans cette étude, une modélisation par éléments finis en grande déformation de la pénétration dynamique de la conduite est présentée. Une technique de type Eulérien Lagrangien (CEL) est utilisée pour développer le modèle éléments finis. Le tuyau est d'abord mis en place dans le fond marin puis subit un mouvement cyclique de faible amplitude latérale. Les résultats des modèles éléments finis sont comparés avec les résultats d'essais en centrifugeuses. D'importantes valeurs de la déformation plastique sont obtenues autour de la canalisation lors du chargement cyclique ce qui nécessite un ancrage suffisant de la conduite. La forme du sol encaissant est différente de celle du tuyau mis en place statiquement.

KEYWORDS: pipelines, dynamic embedment, clay, large deformation analysis.

1 INTRODUCTION

As-laid pipelines are commonly used in deepwater. During installation the as-laid pipeline could be penetrated a fraction of its diameter into the seabed (Bruton et al. 2006), and a soil berm could be formed. The soil around the pipelines provides not only the thermal insulation and hydrodynamic stability to the pipe but also resistance to pipeline walking and lateral buckling during high operating temperature and pressure. Accurate assessment of as-laid pipe embedment is extremely difficult. Depending upon sea state, vessel conditions, pipe stiffness and soil conditions, the pipeline might experience both in-plane and out-of-plane cyclic motion during installation (Westgate et al. 2010, 2012), which causes dynamic embedment of the pipeline.

The penetration of a pipeline under static load can be obtained using bearing capacity theory, analytical solution or finite element techniques. In the current engineering practice, two additional factors are used to estimate the embedment of pipelines: (a) additional vertical force near the TDP (the point where the pipe first touches the soil) due to catenary effects and (b) dynamic lay effects. A number of methods have been proposed in the past to estimate these factors (Carneiro et al. 2010, Oliphant and Yun 2011). For example, Randolph and White (2008) proposed an empirical equation to calculate the touchdown lay factor ($f_{lay}$) using pipe submerged weight, bending rigidity, horizontal component of effective tension, lay angle, water depth and seabed stiffness. The embedment factor for dynamic lay effects ($fdyn$) varies between 2 and 10 (Lund 2000, Bruton et al. 2006). This wide range of variation in this factor makes the assessment of pipe embedment very difficult.

During installation, both vertical and lateral pipe motions can soften the seabed soil near the pipe. Soil softening/remolding together with water entrainment can reduce the undrained shear strength of soil. Field observation (Westgate et al. 2010) and physical modeling using geotechnical centrifuge (Cheuk and White 2011) show that the horizontal cyclic motion, although small amplitude, has a significant effect on pipe embedment.

The main purpose of this study is to conduct large deformation finite element (FE) analysis for dynamic events during the installation of pipeline. Coupled Eulerian Lagrangian (CEL) technique is adopted in the analysis using ABAQUS FE software. Four FE models are developed for two different soils: kaolin and high plasticity clays (plasticity index for kaolin is 34 and for high plastic clay is 100-130, Cheuk and White 2011). The results are compared with the centrifuge test results available in the literature.

2 PROBLEM DEFINITION.

The problem considered in the present finite element (FE) modelling is shown in Fig.1. During laying, offshore pipelines usually penetrate vertically into the seabed due to its self-weight and catenary effect near the touchdown zone (TDZ). The vessel movement from wave loading could cause small amplitude cyclic motions in the x-direction. As the pipeline is under a vertical load ($p_b$), the lateral movement in the x-direction could cause additional vertical penetration as shown by Stage-II and III in Fig. 1.
3 FINITE ELEMENT MODELLING.

ABAQUS 6.10 EF-1 is used in the present finite element analysis. As the embedment of pipe in the seabed is large deformation problem, the conventional finite element techniques in Lagrangian approach cannot simulate the complete process realistically as numerical difficulties are generally encountered for such large displacements. Therefore, in this study the Coupled Eulerian Lagrangian (CEL) technique currently available in ABAQUS FE software is used. In CEL, the soil flows through the fixed mesh without having any numerical issues. The FE modeling using CEL for pipe embedment into the seabed is presented by the authors previously (Dutta et al. 2012 a,b). A soil domain of $8m \times 3m \times 0.04m$ (length $\times$ height $\times$ thickness) is used in this study. The soil is modelled as Eulerain elements and the pipe is modelled as Lagrangian elements. The 1.5 m void space above the soil is required to accommodate the displaced soil mass (Eulerain materials) during pipe displacement. Zero velocity boundary conditions are applied at all faces of the Eulerian domain to make sure that Eulerain materials are within the domain and cannot move outside. However, at the seabed-void interface, no boundary condition is provided so that the soil can flow to the void. That means, the bottom of the model is restrained from any vertical movement, while all the vertical faces are restrained from any lateral movement. The pipe is modeled as a rigid body. During penetration, especially in cyclic loading, the remodeling of soil near the pipe could cause significant reduction in undrained shear strength. Smooth pipe/soil interface condition is used for the present analysis. Mesh sensitivity analysis is also performed and an optimum mesh size of 0.04$m^2/0.04m$ is used (Dutta et al. 2012 a).

The loading is performed in three different stages. First, the geostatic conditions are applied to bring the seabed to in-situ condition. Second, the pipe is penetrated applying a vertical load ($p$) which is the combined effect of submerged unit weight of the pipe and laying effects. In the third step, 40 cycles of lateral displacement are applied using displacement boundary conditions under the constant vertical load $p$, Plastic shear strain develops near the pipe during penetration. In the present FE analyses the degradation of undrained shear strength as a function of plastic shear strain is adopted using the following model (Einav and Randolph 2005 Wang et al. 2009 Zhou and Randolph 2009).

$$s_{pl}=\xi_{um}(kz)_{um}^{+}=\xi_{um}(1-\frac{(1-\xi_{um})\exp(-3\xi_{um})}{1-\exp(-3\xi_{um})})$$

$$s_{pl}=\xi_{um}$$

where $s_{pl}$ is the soil sensitivity, $\xi$ is the accumulated equivalent plastic shear strain, $s_{0}$ is the intact undrained shear strength of soil and $\xi_{um}$ is the accumulated plastic shear strain at 95% undrained shear strength degradation. The variation of $s_{pl}$ with depth is shown in Fig. 1 and the von-Mises yield criteria is adopted.

In this study four cases are simulated and the results are compared with centrifuge test results of Cheuk and White (2008). Two tests (KC-04 & KC-05) are in kaolin clay and two (HP-06 & HP-07) are in high plasticity clay. Table 1 shows the parameters used in the FE analyses. The vertical load $p$ for initial static penetration and during cyclic motion are also shown in Table 2.

<table>
<thead>
<tr>
<th>Pipe</th>
<th>Pipe diameter, D (mm)</th>
<th>Lateral displacement during cyclic motion</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>± 0.05D</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Soil Properties</th>
<th>Kaolin</th>
<th>Clay</th>
<th>High Plasticity Clay</th>
</tr>
</thead>
<tbody>
<tr>
<td>Undrained modulus of elasticity, $E_u$</td>
<td>5000$k_g$</td>
<td>500$k_g$</td>
<td></td>
</tr>
<tr>
<td>Poisson’s ratio, $\nu$</td>
<td>0.495</td>
<td>0.495</td>
<td></td>
</tr>
<tr>
<td>Undrained shear strength at mudline, $s_{mu}$ (kPa)</td>
<td>0.75</td>
<td>0.40</td>
<td></td>
</tr>
<tr>
<td>Gradient of shear strength increase, $k$ (kPa/m)</td>
<td>1.6</td>
<td>2.5</td>
<td></td>
</tr>
<tr>
<td>Submerged unit weight of soil, $\gamma'$ (kN/m$^3$)</td>
<td>6.0</td>
<td>3.0</td>
<td></td>
</tr>
<tr>
<td>Remoulded soil sensitivity, $\xi_{um}$</td>
<td>4.0</td>
<td>1.7</td>
<td></td>
</tr>
<tr>
<td>Accumulate absolute plastic shear strain for 95% degradation of soil strength, $\xi_{um}$</td>
<td>10</td>
<td>10</td>
<td></td>
</tr>
</tbody>
</table>

4 RESULTS.

The pipe was initially penetrated under a static vertical load $p$. The initial static embedment ($w_0$) for this load is shown in Table 2. After initial penetration a small amplitude cyclic lateral load is applied (e.g. Fig. 2 for KC-05, $u = $ pipe lateral displacement) to simulate the first 40 cycles (Stage-I) of centrifuge tests. The normalized lateral resistance for KC-05, where $s_{(w_0)}$ in the horizontal axis is the intact undrained shear strength at pipe invert, is shown in Fig. 3(a) and compared with centrifuge test results in Fig. 3(b). The lateral resistance is slightly higher than that obtained in centrifuge test. This might be due to the limitation of the soil shear strength degradation model (Eq. 1). It is very difficult to measure and model the behaviour of soil near the pipeline under cyclic loading. However, using this simplified model (Eq. 1) in ABAQUS CEL the lateral resistance during cyclic motion is reasonably simulated.

Table 2. Centrifuge test conditions (Cheuk and White 2011).

<table>
<thead>
<tr>
<th>Pipe vertical load, $p$ (kN/m)</th>
<th>Initial static embedment, $w_0/D$</th>
<th>Pipe vertical load at cyclic motion, $p_w$ (kN/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>KC-04</td>
<td>KC-05</td>
<td>HP-06</td>
</tr>
<tr>
<td>1.17</td>
<td>2.23</td>
<td>1.47</td>
</tr>
<tr>
<td>0.08</td>
<td>0.12</td>
<td>0.10</td>
</tr>
<tr>
<td>1.13</td>
<td>2.17</td>
<td>1.43</td>
</tr>
</tbody>
</table>

Figures 4(a),(b) and 4(c) show the lateral resistance for other three simulations. As shown, the shape of the lateral resistance plot is different, which mainly depends on soil shear strength profile, shear strength degradation, sensitivity of soil, and applied vertical load. The depth of the invert of the pipe normalized by pipe diameter (D) with number of load cycle is shown in Fig. 5 for comparison the centrifuge test. the present FE model reasonably simulates the embedment of the pipe with the soil parameters listed in Table 1. Figure 5(a) shows that the depth of embedment does not increase
significantly after 20-30 load cycles for kaolin clay. However, the pattern is somewhat different for high plastic clay as shown in Fig. 5(b) where the pipes continue to penetrate even after 20-30 load cycles.

(e.g. Oliphant and Yun 2011) a combined empirical factor ($f_{d\text{dyn}}$) is also used that accounts for both laying and dynamic effects. Table 3 shows the calculated values of $f_{d\text{dyn}}$ for the four tests simulated in this study. Analyzing field data of a 200 km offshore pipeline in shallow to deep water, Oliphant and Yun (2011) showed that an average value of $f_{d\text{dyn}}$ of approximately 7 could be used for estimation of pipeline embedment. Lund (2000) suggested that the value of $f_{d\text{mon}}$ in the field varies between 2 and 10.

6 EQUIVALENT PLASTIC STRAIN AND BERM SHAPE.

During penetration the soil around the pipeline is softened as a function of plastic shear strain as shown in Eq. 1. The equivalent plastic shear strain at the end of penetration is also used that accounts for both laying and dynamic effects. Table 3 shows the calculated values of $f_{d\text{dyn}}$ for the four tests simulated in this study. Analyzing field data of a 200 km offshore pipeline in shallow to deep water, Oliphant and Yun (2011) showed that an average value of $f_{d\text{dyn}}$ of approximately 7 could be used for estimation of pipeline embedment. Lund (2000) suggested that the value of $f_{d\text{mon}}$ in the field varies between 2 and 10.

![Figure 3. Test KC-05 (a) present study (b) centrifuge test.](image)

![Figure 4. FE results (a) KC-04 (b) HP-06 and (d) HP-07.](image)

5 DYNAMIC EMBEDMENT

In the current engineering practice the effects of laying and dynamic embedment are assessed separately. The lay effect on vertical load ($p$) is obtained by multiplying the submerged unit weight of the pipe by an empirical lay factor ($f_{d\text{lay}}$). The monotonic embedment ($w_{d\text{mon}}$) for this load $p$ is calculated using the bearing capacity theory. The effect of small amplitude cyclic lateral motion is incorporated using another empirical factor known as dynamic embedment factor ($f_{d\text{dyn}}$). Finally, the total embedment ($w_d$) is calculated as $w_d = f_{d\text{mon}} w_{d\text{lay}}$. In some projects

![Figure 5. Pipeline embedment with horizontal cyclic motions (a) Kaolin clay (b) High plasticity clay.](image)
than 95%. The softening has a significant effect on the shape of the berm and soil movement around the pipe, the highly softened displaced soil mass formed flat berms on the top of the seabed extended over a large distance in cyclic loading. In addition, the soil is in contact with the pipe almost up to the top of the berm. However, for monotonic loading the displaced soil mass formed a berm mainly near the pipe and the berm height is more than that of in cyclic loading. That means, the soil deformation in monotonic and cyclic loading is significantly different.

In a parametric study Dutta et al. (2012 b) showed that the effect of softening on the vertical penetration resistance in monotonic loading is not very significant, which is because of less plastic strain developed near the pipe. However, for cyclic loading huge plastic strain is developed in a zone near the pipe which causes significant reduction in undrained shear strength. That means, the zone of considerable softening is higher in cyclic loading. As in offshore the small amplitude lateral cyclic loading near the touchdown zone is commonly encountered from the motion of the vessel, the analyses for cyclic motion with strain softening behaviour of soil will provide more accurate results.

Table 3. Dynamic embedment factor, $f_{\text{dyn}}$.

<table>
<thead>
<tr>
<th></th>
<th>KC-04</th>
<th>KC-05</th>
<th>HP-06</th>
<th>HP-07</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initial static embedment ($w_a/D$)</td>
<td>0.08</td>
<td>0.12</td>
<td>0.10</td>
<td>0.22</td>
</tr>
<tr>
<td>Final embedment ($w/D$)</td>
<td>0.34</td>
<td>0.50</td>
<td>0.48</td>
<td>0.77</td>
</tr>
<tr>
<td>$f_{\text{dyn}}$</td>
<td>4.25</td>
<td>4.16</td>
<td>4.8</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Figure 6. Equivalent plastic strain.

7 CONCLUSION

Large deformation finite element analyses are conducted to assess the embedment of as-laid offshore pipelines in clay. The effects of small amplitude cyclic lateral loading are investigated. The following conclusions can be drawn from this study:

- The Coupled Eulerian Lagrangian (CEL) method currently available in ABAQUS FE software can simulate the pipeline embedment.
- The plastic shear strain near the pipeline in cyclic loading is significantly higher than that of in monotonic loading.
- The shape of the berm depends on type of loading; spread over a large area in cyclic and mounted near the pipe in monotonic loading.
- The softening of soil in a zone near the pipe is significantly higher in cyclic loading compared to monotonic loading.
- Forty cycles of small amplitude lateral loading increased the embedment by a factor of 4-5 of initial static embedment. The embedment is higher in initial loading cycles.

8 ACKNOWLEDGEMENTS

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9 REFERENCES


